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PROCESSING TRANSLATIONAL MOTION SEQUENCES

Daryl 7. Lawton

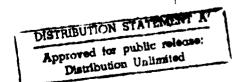
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ABSTRACT

This paper presents a procedure for processing real world image sequences produced by relative translational motion between a sensor and environmental objects. In this procedure, the determination of the direction of sensor translation is effectively combined with the determination of the displacements of image features and environmental depth. It requires no restrictions on the direction of motion, nor the location and shape of environmental objects. It has been applied successfully to real-world image sequences from several different task domains.

The processing consists of two basic steps: Feature Extraction and Search. The feature extraction process picks out small image areas which may correspond to distinguishing parts of environmental objects. The direction of translational motion is then found by a search which determines the image displacement paths along which a measure of feature mismatch is minimized for a set of features. The correct direction of translation will minimize this error measure and also determine the corresponding image displacement paths for which the extracted features match well.



1. INTRODUCTION

This paper develops a procedure for processing real world image sequences from a translating sensor. The procedure is not dependent on an initial matching process for finding image displacements before inferring environmental depth and camera motion. Instead, the determination of the direction of sensor translation is combined with the determination of the displacements of image features and of environmental depth. No restrictions on the shape of environmental objects are required. The procedure has been applied to real world image sequences under several different operating conditions with robust performance.

The processing consists of two basic steps: Feature Extraction and Search. The feature extraction process picks out small image areas which may correspond to distinguishing of environmental objects. The direction translational motion is then found by a search determines the image displacement paths along which a measure of feature mismatch is minimized for a set of features. correct direction of translation will minimize this error MOASHTO and also determine the corresponding displacement paths for which the extracted features match well.

The feature extraction process, which is presented in section

two, finds distinctive points along image contours determined by simple processes which are sensitive to image edges. It finds features which are positioned at points of high curvature along these contours. The technique utilizes contours determined by zero-crossing extraction and image thresholding.

The search process, which is presented in section three, minimizes a simple error measure. This error measure is defined with respect to a unit sphere with each point on the sphere corresponding to a different direction of sensor translation. A given direction of translation constrains the motion of extracted image features to straight lines which radiate from or converge onto a single point. The error measure thus associates with a point on the unit sphere, corresponding to a particular translational axis, a number describing the total extent of feature mismatch along the displacement paths determined by the translational axis. Experiments have shown this error measure to be smooth and with a distinct minimum in a large neighboorhood about the correct translational axis. Because of this, the search process can be quite simple.

The fourth section presents several experiments showing the results of applying the procedure in several different situations. The experiments indicate that the procedure is very robust and applicable to a wide range of real world image sequences.

The fifth section discusses various aspects of the procedure and outlines some applications and extensions.

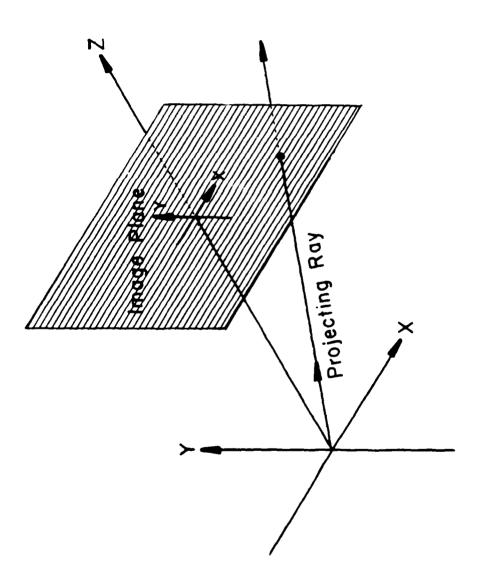
1. 1. Coordinate Sustem

The camera model consists of a planar retina embedded in a three-dimensional Cartesian coordinate system (X,Y,Z), with the origin at the focal point and the optical axis aligned with the positive Z-axis (figure 1). The X and Y axes correspond to the gravitationally intuitive horizontal and vertical directions respectively. The image plane is parallel to the XY plane and at some distance along the Z axis. Positions in the image plane are described using a 2-d coordinate system aligned with the X and Y axes of the camera coordinate system and with the origin determined by the intersection of the image plane and the Z-axis.

The axes of translation are unit vectors based at the origin of the camera coordinate system and are described by two angles (Phi1, Phi2) (figure 2). For a unit vector, \underline{V} , based at the origin, Phi1 is the angle between the (0,1,0) vector and the edge determined by the intersection of the YZ plane and the plane determined by the X axis and \underline{V} . Phi1 thus specifies a plane containing the X axis. Phi2 is the angle between (-1,0,0) and \underline{V} . Note that for all angles a and b, (a,0)=(b,0) and (a,PI)=(b,PI).

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Camera Model

Figure 1.

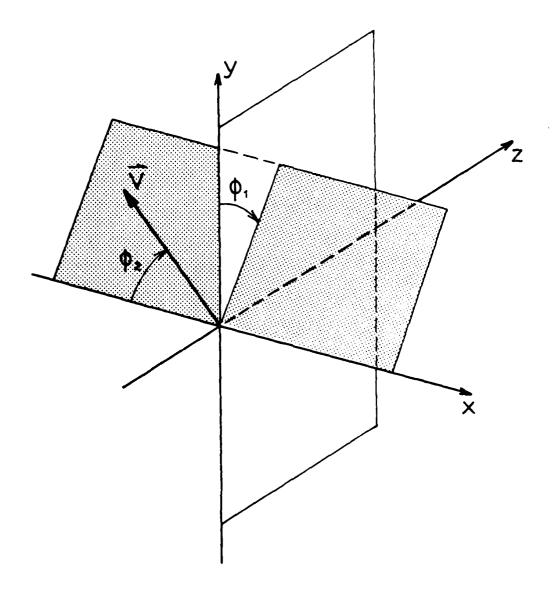


Figure 2. (Phil, Phil) Coordinates

1.2. <u>Translational Motion Properties</u>

It is necessary to have a set of terms for describing the motion of features in an image sequence and the corresponding motion of environmental points. We define Image Displacement Vector to be a two-dimensional vector describing the displacement of an image feature from one image to the An Image Displacement Field is the set of image next. displacement vectors for successive images. Image Αn Displacement Sequence indicates the positions of an image feature over several successive images. Though we are dealing with discrete image sequences, it is often possible to descibe the continuous curve along which an image feature point is moving. This curve is called the Image Displacement Path.

Corresponding to image motions we use a set of terms for describing environmental motions. An Environmental Displacement Field is the set of three-dimensional vectors indicating the positions of environmental points at successive instants. An Environmental Displacement Sequence indicates the position of an environmental point over several successive instants. An Environmental Displacement Path describes the three-dimensional curve that environmental points are moving along for particular motions.

For general camera motion, there are 5 parameters [PRABO, PRAB1] that can be recovered from processing image motion without knowing absolute camera displacement or velocity

(since absolute depth is lost): two parameters for the unit describes the vector (T1(t), T2(t)) which two parameters for the unit translational motion at time t; vector (R1(t), R2(t)) describing the axis of rotation at time and one parameter R3(t) which describes the extent of rotation about this axis at time t. Both of these axes are positioned at the origin of the camera coordinate system The problem of processing image motion resulting from rigid body camera motion can be organized into subcases of increasing complexity, corresponding to the number of camera motion parameters that are unconstrained.

For purely translational motion, the image displacement paths are determined by the intersection of the translational exis with the image plane. If the translational axis intersects the image plane on the positive half of the axis, the point of intersection is called a Focus of Expansion (FOE) and the image motion is along straight lines radiating from it. This corresponds to camera motion towards environmental points. the translational axis intersects the image plane on the negative half of the axis, the point is called a Focus of Contraction (FOC) and the image displacement paths are along straight lines converging towards it. This corresponds to camera motion environmental The from points. awau intersections of axes parallel to the image plane are points at infinity and are treated as FOEs.

Given the direction of translation and image displacements, the relative depths of points can be computed by solving the inverse perspective transform [ROG76]. Relative depth can also be inferred from the position of a feature and the extent of its displacement relative to an FOE or an FOC. This relation is expressed as

$$\frac{D}{\Delta D} = \frac{Z}{\Delta Z}$$

where Z is the value of the Z component of an environmental point at time t+1, del Z is the extent of environmental displacement along the Z axis from time t to time t+1, D is the distance of the corresponding image point from the FOE or FOC at time t and del D is the image point's displacement from time t to time t+1. Thus, the Z value of an environmental point can be recovered from image measurements in units of del Z, or what has been termed <u>Time-Until-Contact</u> by Lee [LEE76].

The set of all possible translational axes describes a unit sphere called the <u>translational direction sphere</u>. The procedures below are defined with respect to this sphere, rather than the image plane itself, for reasons described in section 5.2.2.

1.3. Previous and Related Work

Gibson[GIB50,GIB66] was among the first to study the importance of the structure of optic flow fields in the

importance of the FOE in the translational case. This work was extended by Purdy and by Lee [LEE76, LEE80]. Lee analyzed the computation of important control information during translational motion, such as time-until-contact, braking information, and environmental depth in a natural coordinate system. However, recent work by Beverly and Regan [REG78, REG79] indicates that an alternative mechanism may be used in humans for determining the direction of translation than extraction of a FOE or FOC.

Work in processing dynamic images [HUA81, MART79, NAG81a. THO81, ULL81] can be roughly divided into a set of techniques for determining the changes in a sequence of images and a set for interpeting these transformations. Determining image motion has involved work in change detection, correlation based matching techniques [QUA71, HAN74, LEV73], relaxation based matching techniques [BAR79, PRABO], region matching [NAG78 RAD813; image differencing [JAIB1]; spatia temporal analysis of the image gradient constraints of locally uniform motion [THOBO] and smoothly varying image motion [HDR81, GLA81].

The interpetation of image motion can result in a variety of descriptions such as determination of the occurrence and location of change [MAR79]. These include image segmentations based on common motion [THO80]; the recovery of camera motion parameters and the shape of environmental objects; and more

qualitative descriptions at a level compatible with natural language descriptions [BAD76, TS080, O'ROUB0]. Particularlu relevant here is work with the recovery of camera motion parameters from an image sequence. Ullman. [ULL79] demonstrated the minimal number of observable points necessary to obtain a solution over time. Roach and Aggarwal [ROABO] investigated noise robust computations of the camera motion parameters. Prazdny developed techniques for decomposing optic flow fields [PRA80] and displacement fields [PRA81] into their rotational and translational components. The latter result has been given a particularly simple algebraic formulation by Nagel [NAGB1b]. Tsai and Huang [TSAB1] have investigated the simplifications in determining camera motion parameters by restricting the interpretation to planar surface patches.

Williams [WIL80] was the first to develop algorithms for interpreting complex natural images produced by an optic sensor translating relative to environmental objects. This work consisted of two processes: one for inferring the direction of translation given environmental depth information and the other for inferring depth given the direction of motion. These processes used an error measure describing the consistency of depth information and the inferences of feature motion along image displacement paths. His work indicated that these two processes, for inferring depth and the translational axis, could be combined.

The primary weakness of Williams' work was the necessary at demonstrated planar surfaces one restriction to orientation. Additionally, the processing is quite complex environmental depth nor the direction of neither known -- --involving segmentation, translation is resegmentation, and coordinating the processes for inferring depth and for inferring the direction of translation. presented here requires no restrictions on method orientation of surfaces or shape of environmental objects, and involves only a simple procedure for evaluating an error measure. It also indicates that the direction of sensor motion should be determined prior to, or concurrently with, environmental depth.

The determination of the vanishing point in a static image is closely related to determining the direction of translation because the FOE is the dynamic analogue of the vanishing point. In perspective projection, parallel lines in the environment map onto lines radiating from a vanishing point in the image. For translational motion, the environmental motion paths correspond to the parallel lines in the perspective case. Techniques for extraction of a vanishing point have been developed by Kender [KEN79] and Kitihashi [KIT80]. The use of the Hough transform in this work is similar to the global sampling of the error measure used below.

2. FEATURE EXTRACTION

The feature extraction process is used to determine small areas (sometimes called image points or features) in an image distinct from neighboring areas. This distinctiveness limits the potential matches of these image areas, and possibly reflects a correspondence to actual and significant points in the environment, such as points of high curvature on object boundaries, texture elements, surface markings, etc. (However some features, termed false features, will result from noise, occlusion, and light source effects and have behavior which is currently difficult to interpet). Features can be represented either as arrays of numbers extracted directly from an image, or as parameterized tokens describing local image properties. In this paper, we refer to features exclusively as small arrays of data values centered at some point in an image at some time t.

Following Moravec [MOR77, MOR80], the method of feature extraction used here is based upon finding image areas which are significantly different than their neighboring areas. Using a correlation measure bounded between 1 (for perfect correlation) and O. the <u>distinctiveness</u> of a feature is 1 minus the best correlation value obtained when the feature is correlated with its immediately neighboring areas (see the correlation measures in section 3.1.). Selecting good features then requires finding the local maxima in the values

We have extended this approach somewhat by constraining the neighborhoods over which the features are selected to contours determined by other global processes, such as zero-crossing extraction and thresholding, which are sensitive to edges

2.1. Feature Extraction Using Zero-Crossings

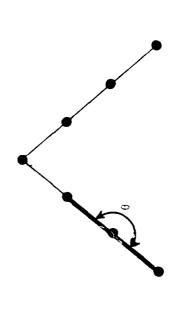
The use of zero-crossings to determine significant image contours at different levels of resolution has been proposed and extensively studied by Marr et. al. [HIL80, MAR80]. In this processing an image is convolved with Gaussian-Laplacian masks ((del)**2g) of different positive widths and thresholded at zero to determine zero-crossing contours. These contours are significant since they correspond to the points of greatest change in the convolved image. The distinctiveness measure can be applied to points along these contours in the convolved image, with the local maxima determining the position of potential features. This generally has the effect of finding points of high curvature along the zero-crossing contour, although points apparently corresponding to local occlusion vertices and weak maxima will also be extracted

Many of the weak features which are local maxima of distinctiveness can be removed by suppressing those which are at points of low curvature along the zero-crossing contours

For features which are local distinctivness maxima, we approximate the curvature along the contour by the inner product of the normalized vectors describing the relative positions of adjacent local maxima along the contour (figure 3). These values are then thresholded between 1.0 (corresponding to high curvature) and -1.0 (corresponding to low curvature).

Use of zero-crossing based features requires specification of the sizes of the convolution masks that are employed, and deciding whether to position extracted feature points with respect to the unprocessed image or the convolved images. is usually beneficial to use masks of various widths for sensitivity to features at different levels of resolution. The processing described below can be applied independently to the pairs of successive images formed by convolving the successive images with two such masks. Alternatively, features can be extracted from the original, unfiltered image at the positions where features were determined in the convolved images, though experience with large masks has shown that this approach can position features significant distances from their apparent position in the original image.

The images in figure 4a and figure 4b were taken from a gyroscopically stabilized movie camera held by a passenger in a car traveling down a country road in Massachusetts. They are 128x128 pixel images with 6 bits of resolution in intensity and will be referred to as the <u>roadsign images</u>.



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Figure 3. Curvature Approximation for Features Along an Extracted Contour





Figure 4c shows the zero-crossings extracted from the initial ROADSIGN image using a (del)**2q mask with a width of 5 The distinctiveness values were computed pixels. features which were 5x5 pixel arrays extracted from the convolved image and centered on pixels which were adjacent to the zero-crossing contour and of positive value. features were correlated, using Moravec's norm (see section 3.1), with their 8 immediately neighboring features. distinctiveness measure for a feature was set to 1 minus best correlation obtained in its neighborhood, excluding itself. Figure 4d shows the local maxima in the distinctiveness measure positioned with respect to the zero-crossing contour. Note that the features are centered on pixels adjacent to the contour and not on the contour itself. Figure 4e shows the results of suppressing low-curvature points using a threshold set to -0.8 (corresponding to an angle of 143.13 degrees).

2.2. Feature Extraction Using Threshold Contours

Image contours can also be determined by thresholding. The values of the threshold can be determined in a variety of ways: such as using fixed increments, finding peaks and valleys in the image intensity histogram, or using techniques sensitive to image contrast produced using a particular threshold [KJH81, WES75].

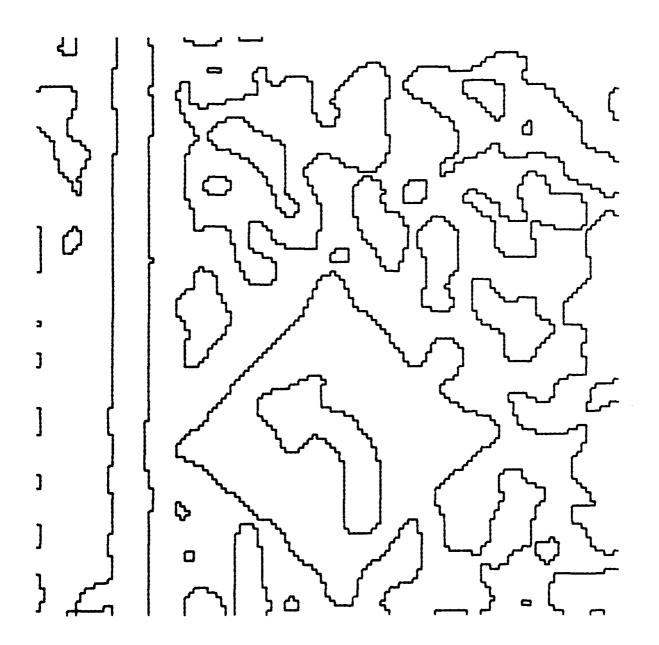


Figure 4c. Extracted Zero-Crossings of Roadsign Image 1

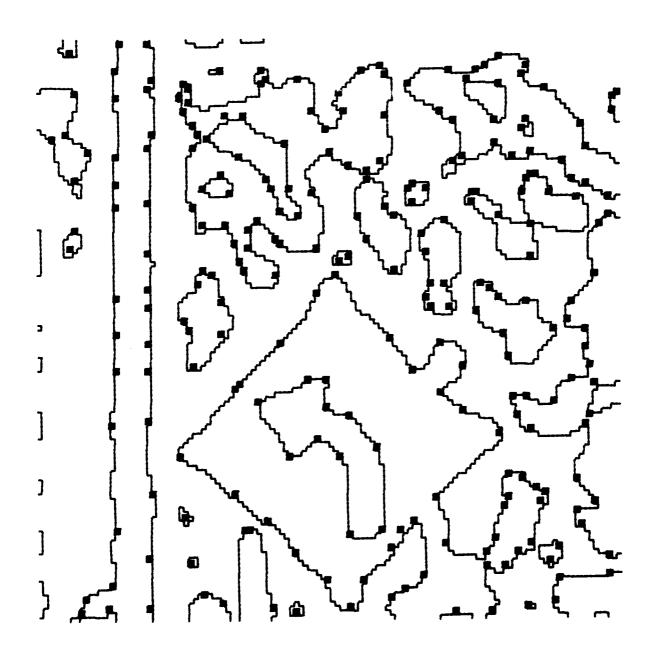


Figure 4d. Distinctive Feature Positions with Respect to Zero-Crossing Contour

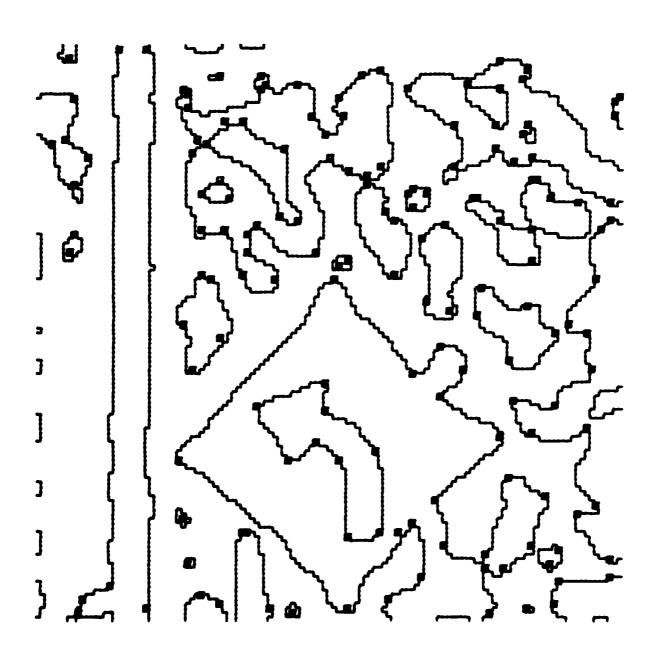
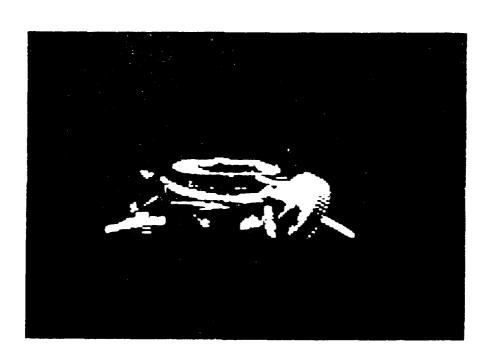


Figure 4e. Distinctive Feature Positions After Low-Curvature Suppression

The images in figure 5a and 5b were produced from a solid state camera held by a robot manipulator translating toward some industrial parts lying on a table. The images were initially 512x512 pixel images with 7 bits of intensity resolution and were averaged down to 128x128 pixel images with 6 bits of intensity resolution. These will be refered to as Analysis of the image intensity the industrial images. the procedures described in [KOH81], histogram, using determined a clear break in the histogram at an intensity level of 10 in the image. This corresponded to separating the dark background and the brighter objects in the scene. Figure 5c shows the extracted contour and figure 5d the local maxima in the distinctiveness measure of image features centered on pixels adjacent to the contour and of intensity value greater than or equal to ten. Figure 5e shows the extracted feature points after low curvature suppression using a threshold set to -0.8 (corresponding to angle of 143.13 degrees).



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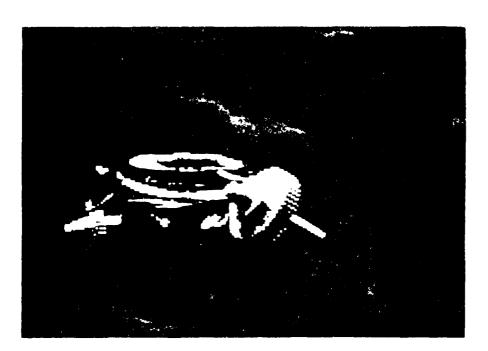


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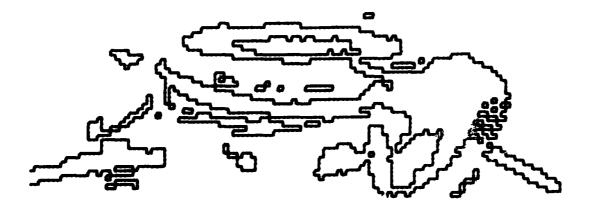


Figure 5c. Extracted Threshold Contour of Industrial Image 1



Figure 5d. Distinctive Feature Positions with Respect to Threshold Contour

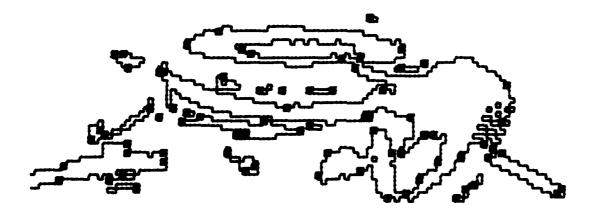


Figure 5e. Distinctive Feature Positions After Low-Curvature Suppression

3. SEARCH PROCESS

The search process minimizes an error measure which describes the extent of mismatch for extracted features along the image displacement paths determined by a hypothesized translational axis. For example, figure 6 shows an FOE determined by a potential translational axis and the image displacement paths it determines for some extracted features. Also shown is the match profile for a particular feature along a segment of its displacement path with respect to features positoned in the succeeding image. The adequacy of a proposed translational axis is measured by the strength of the matches that the extracted features have along these paths. This suggests finding the best match for each feature along the image displacement path determined by a translational axis and then summing the extent of error in these best matches for the error measure.

Developing this error measure requires a measure for the degree of match between features and an interpolation process for determining positions along an image displacement path. Each of these can be implemented in various ways with the choices generally involving a trade-off between the speed of evaluating the error measure and the precision with which the translational axis can be determined.

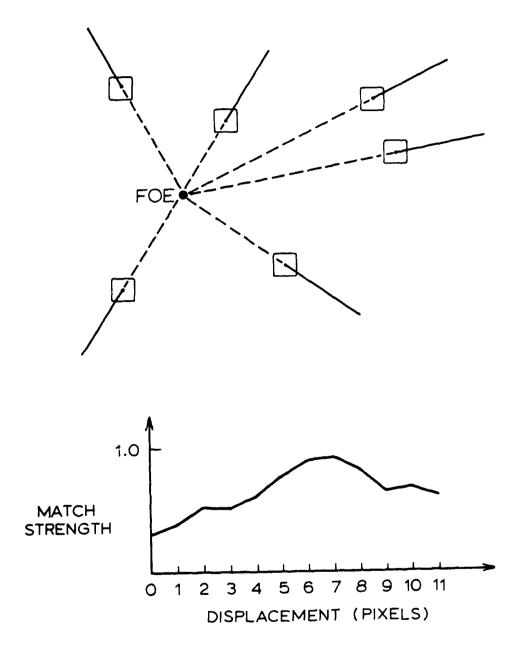


Figure 6. Feature Displacements for a Potential Translational Axis

3 1 Match Metric

There are several metrics for similarity of nxn pixel features of the form A(i,j) and B(i,j), where i ranges from 1 to n and j ranges from 1 to n. We have utilized:

Normalized Correlation

$$\frac{\sum\limits_{i = j}^{\sum} A(i,j) \times B(i,j)}{\sqrt{\sum\limits_{i = j}^{\sum} A(i,j) \times A(i,j)} \times \sqrt{\sum\limits_{i = j}^{\sum} B(i,j) \times B(i,j)}}$$

Moravec Correlation [MOR77]

$$\frac{\sum\limits_{i}\sum\limits_{j}A(i,j)\times B(i,j)}{(((\sum\limits_{i}\sum\limits_{j}\Lambda(i,j)\times \Lambda(i,j))+(\sum\limits_{i}\sum\limits_{j}B(i,j)\times B(i,j)))/2)}$$

Normalized Absolute Value Difference

1.0 -
$$\left(\begin{array}{c} \sum_{i \neq j} \operatorname{abs}(A(i,j)-B(i,j)) \\ \frac{\sum_{i \neq j} \sum_{j} \Lambda(i,j) + \sum_{i \neq j} \sum_{j} B(i,j)}{i \neq j} \right)$$

All of these measures have a value of 1 for a perfect match. Of these, the first choice is the most conventional, the second a good approximation to the first, and the third is the quickest to evaluate.

3.2. Interpolation Process

The interpolation process approximates the potential displacements of a feature from an initial image into a Depending on the accuracy required, succeeding image. image displacement path can be positions along the approximated roughly by setting the coordinates of feature's position to the nearest integer value, or more accurately by performing a subpixel interpolation of the feature at each of a set of selected positions along the image displacement path. The basic trade-off is between speed and accuracy, with subpixel interpolation being a more expensive computation.

3. 3. Error Measure

The error measure associates with a point on the direction of translation sphere a number describing the quality of feature matches along the image displacement paths determined by the corresponding translational axis. This error value is computed by first finding the best match for each feature along a segment of the image displacement path determined by the translational axis using one of the normalized match metrics above. Each of these values is then subtracted from one, and all the resulting values are added together to form an error measure. Thus, for a set of N features in an initial image, a hypothesized translational axis, and use of one of

the match metrics above, the error measure is

$$\sum_{i=1}^{n} (1.0 - bestmatch(i))$$

where $\underline{bestmatch(i)}$ is the best match value associated with feature i along the image displacement path determined for it by the hypothesized translational axis.

The error measure was computed in two forms in the experiments below: a <u>fast evaluation</u> form and a <u>precise evaluation</u> form. The fast form uses the absolute value norm and the nearest integer approximation to determine feature position along the image displacement paths. The fast form is useful for evaluating image sequences with several extracted features to determine the rough position of the global minimum. However, the fast form is not adequate for fine determination of the translational axis because it does not vary smoothly with respect to small changes in the position of a translational axis, due to the nearest integer approximation for feature position.

The precise form of evaluation uses the Moravec norm and bi-linear interpolation. It has been found to vary smoothly with respect to small changes in the position of a translational axis.

3.4. Search Organization

sampling of the error measure determines the rough shape of the error surface, then a local search determines the minimum. The local search begins at the position where the minimum value was determined by the global sampling. The procedure used for the local search is steepest descent with a diminishing step-size. That is, the steepest descent procedure begins with a initial fixed step size and determines a local minimum using it. The step-size is then reduced and the prodedure repeated until the step-size is at the desired resolution for the determination of the translational axis. In the experiments below the initial step-size was set to 0.1 and then reduced successively to 0.025 and 0.005 radians.

As will be seen in the following experiments, the error measure is smooth, with a single minimum in a large neighborhood around the correct translational axis. Thus, the global sampling can be quite sparse or the initial step size of the local search quite large.

4. EXPERIMENTS

The following experiments were performed using the roadsign and industrial image sequences introduced earlier. They cover a wide range of situations. The first experiment involves determining the translational axis for the industrial image sequence using the features indicated in figure 5e. In this sequence the translational axis intersects the image plane in a visible portion of the image. The second experiment involves processing the industrial image sequence using a small number of features that are positioned across the initial image of the sequence. The third experiment involves processing the roadsign image sequence using the features extracted at the positions indicated in figure 4e from the initial, unconvolved image. In this sequence the intersection of the translational axis and the image plane is not in the visible portion of the image. The fourth experiment involves processing the roadsign image sequence, but using the features extracted prior to low-curvature suppression. This has the effect of introducing weak and spurious features into the error measure computation. The fifth experiment involves processing the roadsign images using features extracted from a small area of the initial image.

In all of the experiments, the maximal displacement along an image displacement path was set to 10 pixels. Displacements were in increments of 1 pixel along the image displacement

paths. Features were 7x7 pixel arrays centered at the positions in the indicated figures.

For each experiment, the results of processing are contained The first two (tables a and b) indicate the in 3 tables. values of the error measure during the global sampling of points using a fixed angular increment (equal to PI/10 or 0.31416 radians or 18 degrees) on the direction of translation first o f these tables corresponds to sphere. translational axes which intersect the image plane at FOEs The second basically corresponds to those which intersect the image plane at FOCs. Recall that the Phi1 determines a plane containing the X-axis of the camera coordinate system and Phi2 refers to positions of unit vectors in such a plane.

The third table (table c) shows the minimal value determined by the global sampling process and the successive values of the error measure determined during the local search. In this table, the position of the translational axis is referred to in terms of (X,Y,Z) camera coordinates, in addition to (Phil,Phi2) coordinates, so that translational axes computed under different situations can be compared.

4.1. <u>Industrial Images</u>

The procedure was applied to the industrial images—using—the

features extracted at the positions shown in figure 5e. Tables 1a and 1b show the global sampling of the error measure using the fast form of evaluation. Note the minima at Phi1=1.57080 and Phi2=1.25660. Table 1c shows the successive values of the local search using the precise form of evaluation. The determined translation axis is (-0.13875, -0.09887, 0.98538). The image displacements determined for these features is shown in figure 7.

4.2. Industrial Images with Selected Features

The procedure was again applied to the industrial image sequence but using features which were selected by hand from those indicated in figure 5e. The positions of these 8 features are shown in figure 8.

Tables 2a and 2b show the global sampling of the error measure using the precise form of evaluation. Note the minima at Phi1=1.57080 and Phi2=1.57080. Table 2c shows the successive position determined by the local search. The determined translational axis was (-0.15438, -0.07896, 0.98485). This corresponds to an angular difference of 0.0253 radians $(1.4505 \, \text{degrees})$ with respect to the axis determined in experiment 1.

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Phi⊺	Phi2	x	Y	2	Error	Stepsize
1.5708	1.2565	-0.30905	0.00000	0.35105	*14.446*	
1.6703	1.4565	-0.11395	-7.nan+3	1.98852	3.5456	2.1
1.6708	1.4316	-0.13875	-0.09887	3.98533	3.5313	0.025
1.6708	1.4316	-0.13875	-0.09887	0.98538	3.5313	0.005

Table 1c

NOTE: The * denote that this value was determined using the fast firm of evaluation. The others were determined using the precise form.

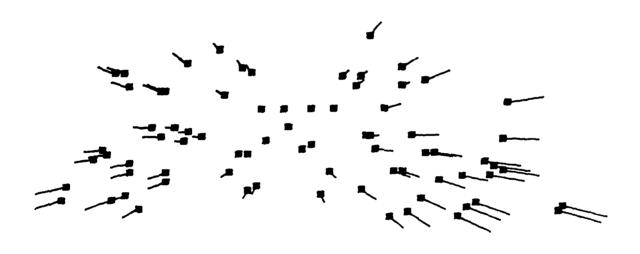


Figure 7. Image Displacements for Industrial Image Sequence

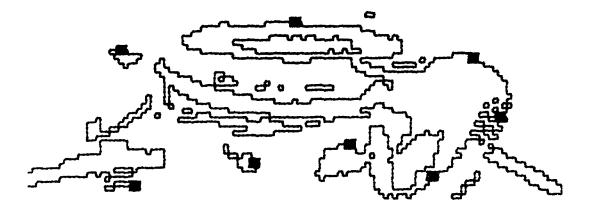


Figure 8. Selected Features for Industrial Image Sequence

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		· · ·				1,64-7,1	3, 5,	1.6218	1.4879	1.775
e Te Co		7 . 7		7.74.7	16491		, Kina i i	1.4645	1.5354	-
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Phi	Phi?	Х	Y	Z	Error	Stepsize
1.5708	1,3708	აიიიი	3.30000	1.00000	0.57098	
1.6708	1.3708	-0.19867	-0.09785	0.97517	0.19955	1.1
1.6458	1.4208	=>.149#1	-0.07481	0.98599	0.17475	*, %, *
1.6508	1.4154	-0.15438	-1.07896	0.98485	0.17410	

Table 2c

4.3. Roadsign Image Sequence

The procedure was applied to the roadsign image sequence using the features extracted at the positions indicated in figure 4e. Tables 3a and 3b show the global sampling of the error measure using the fast form of evaluation. Note the minima at Phi1=2.51330 and Phi2=0.62832. Table 3c shows the successive values of the local search using the precise form of evaluation for the error measure. The translational axis determined by this process is (-0.83738, -0.42043, 0.34933). The image displacements for the feature points shown in figure 4e consistent with this translational axis are shown in figure 9.

Given the direction of translation and image displacements. the relative environmental depths of image points can be recovered by the simple relation in equation 1. When image displacements are small, the inferred depth values can be quite erratic due to sensitivity to small numbers in the denominator in the left hand side of equation 1 For this reason, it is necessary to keep track of the displacements over several successive images with concurrent updating of the inferred depth values. This was done using a sequence of four successive images from the roadsign sequence beginning with roadsign images 1 and 2 and using the features from image 1 at the positions in figure 4e. The position of the translational axis determined from images f(t) and f(t+1)was used as the initial value in the local search for

		, ,.	41.7		1 27			J. 1986. E	1945	2.53.55	2.87740
		C486.4	4.5174	7.486.5	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 2 1 37 1 1 1	7.2765	6.471	4.6319	4.2845	3.3776
	11415		5.2463	7.4334	ं होते हैं	er er	1.2.31	9.8010	9.8676	10.000	10.008
	0.52832		તું તાલું કું જો તાલું કું	7.1224	,) . t . p		9.6247	9.7504	9.8:16	10.097	9.9926
	e # C * * *		7247	6.577	26.4	1 T	7.34.57	9.4924	9.7882	10.320	6.9659
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			#6; > · :	3.795.5	ે. ૧૦% - ૯	5.43.1	6.8211	8.0255	8.7509	9.0412	9.5052
	्र इ. इ.		କ୍ରନ୍ତ ୧୯	3, 1293	и. 3846	6.0775	7.126.1	7.4031	8.8168	9.1253	6.5460
						Table ka					
						Ph i 2					
		3.141.9	3.45575	3.7699:	4.08407	4.39823	4.71238	5.02654	5.34076	5.65486	5.96902
	5.00000.6	11.201	6.4869	8.0216	9.2004	10.242	10.942	11,006	11.869	11.920	11.276
	0.31416		10.762	16. 198	9.5297	8.1033	7,3353	6.5041	5.0061	3,9616	3.5378
	0.52832		10.956	10.793	9.9145	8.7336	7.2365	6.3875	5.2799	4.2700	3.8493
	0.94248		11.139	11.040	10.623	9.5921	8.2331	7.0199	5.6895	4.6911	4.2697
Pr.1.1	1.25660		11,169	11,196	11.066	10.284	9.3429	8.1211	6.7743	5.2348	4.5115
	1.57080		11.202	11.295	11.331	10.970	10.241	6950.6	7.3829	5.6944	4.9589
	1.88500		11.200	11.335	11.639	11.157	10.921	9.4845	7.9038	6.1586	5.3944
	2.19910		11 221	11.540	11.756	11.742	10.882	9.9751	8.1577	6.8129	5.7575
	2 82740		11 253	11.000	11 951	11 285	10.939	10.347	9.0042	7611.7	6 3130
			(, ,				000.	110.01	9.3100	0.000	6010.0

Table 3b

Phi'	Phil	X.	Y	•	Error	Ctepsize
2.5133	0.62830	-1,40902	-3.4 ^{76.6} 4	्. २४५४	*3.70%;*	
2.5131	0.52832	-1.36366	-0.40732	n. 2962£	1.21131	3.3
2.4383	3.57412	-1,82738	-3.41541	1.35352	4.27767	1.125
2.4433	ويهجموه	_3,43738	4/143	3.:44.3	5,29765	2,326

Table 3c

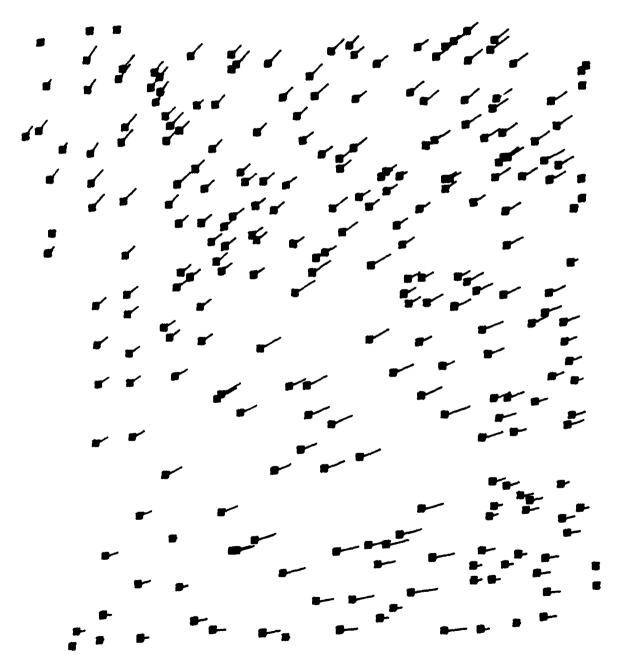


Figure 9. Image Displacements for Roadsign Image Sequence

determing the translational axis for images I(t+1) and I(t+2)

The displacements of all features along the contour in figure 4c were determined along the image displacement paths determined by the translational axis found for images I(1) and I(4). From these displacements the depth values for image points along the contour were computed using equation !

The roadsign sequence is particularly nice for presenting depth processing results because the three environmental objects in the images are at three distinct depths shown in figure 10a by the three distinct clusters in the histogram of the depth values calculated for the points along the contour. The units in the histogram are cummulative time-until-contact values. That is, the depth is given in units of the displacement of the camera from I(1) to I(4)along the Z-axis. From left to right, the first peak corresponds to the sign, the second to the pole, and the third to the trees. As can be seen, there is a wide range of depths associated with the trees. Mapping these clusters back onto contour points from figure 4c yields: the boundary shown in figure 10b (the sign), the boundary shown in figure 10c (the pole), the boundary segment shown in figure 10d (the trees) Points near the image boundary of I(1) were ignored because the processing did not take into account occlusion effects along the image boundaries.

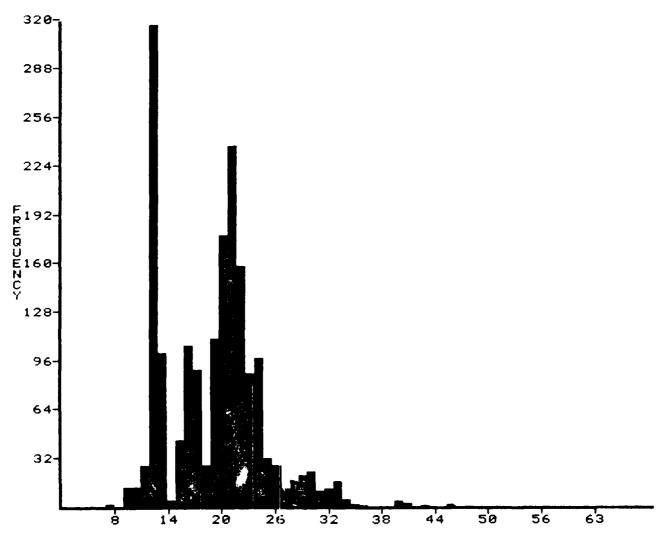


Figure 10a. Depth Histogram

Figure 10b. Image Points in Histogram Cluster Corresponding to the Sign



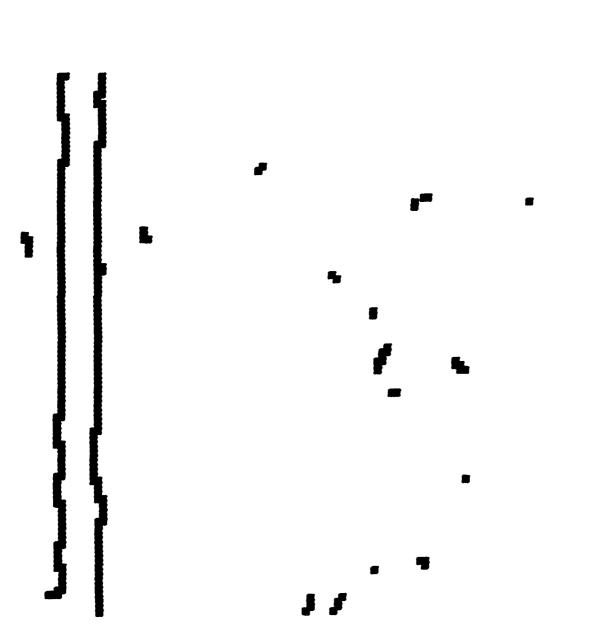


Figure 10c. Image Points in H stogram Cluster Corresponding to the Pole

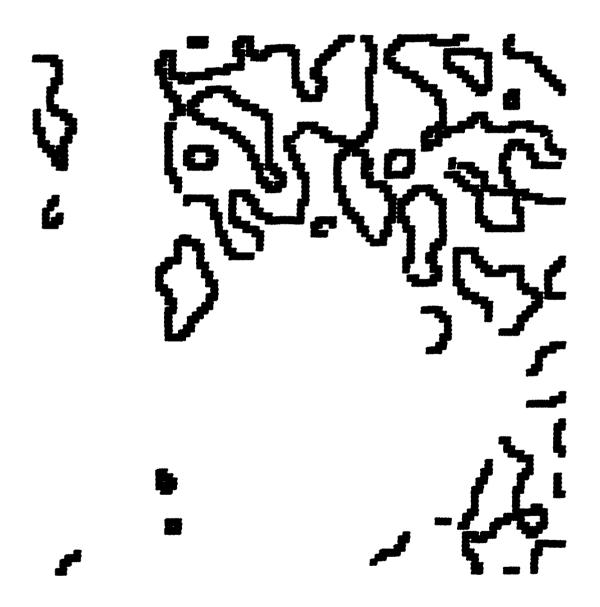


Figure 10d. Image Points in Histogram Cluster Corresponding to the Trees

4 4 Roadsign Sequence with Redundant Features

The procedure was applied to the roadsign image sequence using the features which were extracted prior to low-curvature suppression. The positions of these features is shown in figure 4d. This has the effect of including several weak and false features in the evaluation of the error measure.

Tables 4a and 4b show the values of the global sampling of the error measure using the fast form of evaluation. Note the minima at Phi1=2.51330 and Phi2=0.62832. Table 4c shows the successive values of the local search. The determined translational axis was (-0.82909, -0.42281, 0.36585). This corresponds to an angle of 0.0186 radians (1.0676 degrees) with respect to the axis determined in experiment 3.

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1.5	0.31415		0.941	1.1.449	14.147	16.669	18.318	18.34	18.94	14.546	14.6 21
-			9.54.5	11,503	14.5.14	17.674	18.0⊀0	18.316	19.146	13.644	14,541
	क्षा महार		0:/0.6	11.006	17.474	5.1.5	16.915	17.39%	13, 191	14.54.	19,40
	1.75060		3.41.5	9.417	1.14.	14.141	15,8%	17.581	18.212	19, 317	1.1
	7		7.505.7	7.54.20	9.77.4	12.076	15, 400	ਜ਼. ਬ. ਪ	17. 18.54	1777	
	1.85500		6,6899	6,.7600	8.3045	11.721	13.745	16.95.	17.843	13.489	17.11.1
			ń. ભા9 }	4, 4, 1,	A 6744	10,500	13,197	382.31	17.7.5	34.430	1.6
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	C#1. F.		5.5354	5,2061	7.5152	11,446	14.097	15, 655	7.04.55	15, 441	
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						Phis					
		3.14159	3.46575	1.76991	4.69467	4. 19823	4.71238	5.02654	0.040	45 B 34	
		(##Z / / /	21.903	21.164	19,254	15,980	14.741	10.76	#6577	· · · · · · · · · · · · · · · · · · ·	
	7.31416 ;		22.0.7	21.512	19.503	15.250	14.012	10, 8, 11	F. 1950	B 2 4 5 7 4	3. 34.
**	0.62832		22.284	21.998	19.765	14. 375	1, 4433	10,540	B. 100	10 x 2	1111
	1.94246.		22.615	52,309	20.363	16.019	13.624	11.444	Trust 6 . 5	7.491.7	- x
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	5.1991.5		15.634	24.058	22.176	18.767	16.346	15,663	15.34	7.7	
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Table → a

4.5. Roadsign Subimage

The procedure was again applied to the roadsign image sequence with features restricted to the rectangular area shown in figure 11 correponding to texture in the distant trees

Tables 5a and 5b show the values of the global sampling of the error measure using the precise form of evaluation. Note the minima at Phi1≈2.19910 and Phi2≈0.62832. Table 5c shows the successive values determined by the local search the translational axis is determined to be (~0.84281, -0.42928, 0.32465). This corresponds to angles of 0.0267 radians (1.5341 degrees) and 0.0439 (2.5155 degrees), with respect to the translational axes determined in experiments 3 and 4 respectively.

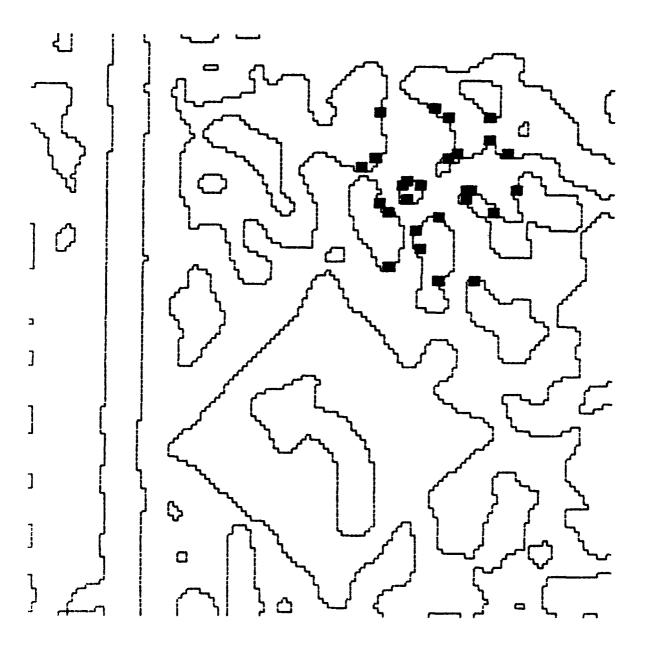


Figure 11. Features in Restricted Subarea of Roadsign Image 1

Phi

		0.31416	2.60842	0.94248	1.25660	1.57080	1.88500	2.19910	2.51330	2.82740
		3.04936	0.75,269	#17.5 # 15	0.46814	0.51525	0.52039	0.50438	0.50165	0.49133
•					0 4€ 44€	0.50514	0.52232	0.50468	0.50000	0.49018
					3. 45971	0.4685,5	0.51958	0.50173	0.43779	0.48276
		V		21 37 17	9.26425	0.41561	0.43856	0.48696	0.47778	0.47140
		1.151.4	1, 145,54 1	1.1534	9.11865	0.12577	0.25988	0.36790	0.44363	0.45981
		38 CC - 1	4.645.55	1,07	3, 67 36	0.11472	0.24358	0.29792	0.36770	0.44106
	-	1.101.75	0.06857	0.065 35	6.10172	0.16910	0.25533	0.29494	0.33419	0.42238
	-	3.00.00	7.05,391	6.08383	0.13701	0.20505	0.26458	0.7406.2	0.32680	0.40534
		3.38336	2.06114	5,10534	0.15614	0.23254	0.27384	0.28820	7. 32911	0.40005
7		₹¢	ୀ, ମର୍ଷ୍ଟ୍ରଥ	0.11949	5,18551	0.25237	0.27365	2920	0.33585	0.40410
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		0.58630	1.13,16	5.6.1143	11594	167691	1.60047	# (C. 40.3.38	0.205.49
		0.59634	2.61354	5.61862	63.740	7.62639	9.61177	37	7, 385.0	0.74.53
		0.60470	0.51687	Capoxin	3.6 /15	1. f is 4.	7.60736		5: #15:C	1,256,1
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k 3 of 1 it.

Phi!	Phi2	X	Y	Z	Error	Stepsize
2.1971	0.62832	-0.80902	-0.34549	0.47553	0.059910	
2.2991	0.62832	-0.80902	-0.39123	0.43867	0.059542	0.1
2.4741	0.57832	-0.83738	-C.42930	0.33837	0.059288	0.025
2.4941	0.56832	-0.84281	-0.42928	0.32465	0.059269	0.005

Table 5c

5. <u>DISCUSSION</u>

This paper presents a simple and robust procedure for determining the direction of environmental motion and image displacements in image sequences produced by a translating sensor. The procedure is robust in several different ways. It is resilent with respect to weak and false features. It is not dependent on identical features being extracted in successive images prior to matching. It can use a small number of features positioned across an image surface or a small number of features from a limited area of the image.

The primary difficulty with real-time implementation is expense of performing the interpixel interpolation for fine resolution and of performing correlations on features which are arrays of pixels. The computational limitation is the speed with which a feature can determine and evaluate potential matches given a specified translational axis. These computations can be carried out in parallel amoung individual features. The expense can be lessened somewhat through the use of higher resolution images (to lessen the need for interpixel interpolation), use of the absolute value norm, and by sampling images at a rate sufficient to limit the extent of feature displacements between images. Additionally, if the direction of sensor translation is changing slowly, information from processing preceeding images can be used to speed up the procedure when applied to succeeding images.

is also possible to modify the procedure so that feautres are extracted from both images and correlations are performed only at the positions where features have been extracted in the succeeding image. This would probably affect the robustness and resolution of the procedure. We hope that real—time implementation will eventually be possible with special purpose, highly parallel architectures.

In the remainder of this section, we review some specific aspects of the procedure and outline some potential extensions and applications.

5 1. Feature Extraction

Since the procedure's performance is does not degrade severely due to the occurrance of poor features, the type of feature extraction used in probably not critical. Nonetheless, the feature extraction process used here could be extended in many ways. The low-curvature suppression could take into account boundary length along a contour between distinctiveness maxima to determine whether to suppress or generate a feature for further processing. It may also be possible to determine points of high curvature along the boundary with out having to walk along the contour by using operators which can directly measure curvature [KITC80].

Another useful extension would be to use information

determined from the extraction of the translational axis to isolate false features. This could involve removing those features which have weak matches from the error measure calculation once a translational axis has been determined and re-evaluating. Alternatively, the depth inferences could be used to isolate the positions of potential false features by noting discontinuities in depth along an extracted contour Extracted features could be removed from the re-evaluation of the error measure if they are at or near such positions. Another type of feature which can affect the evaluation of the error measure are those near an FOE or FOC which is contained in a visible portion of the image. Such features tend to move very small amounts along their image displacement paths and hence require fine interpolation to determine their best matches.

5. 2. Search Process

5. 2. 1. Properties of the Error Measure

In the experiments, the error measure has a distinct global minimum at the point on the unit sphere corresponding to the correct translational axis. It is expected to have such behavior generally because it is very unlikely that translational axes that are far from the correct position will define image displacement paths that simultaneously allow good matches for many features. Thus competing candidates for the

global minimum should not be widely separated.

The error measure is affected by both non-distinctive and false features. Non-distinctive features will match well for many different translational axes. Large numbers of these weak features will flatten the response of the error measure. False features will also distort the error measure since they will often have their best matches with incorrect translational axes.

The effects of these poor features should be compensated by the agreement of good features. Every one of the good features will tend to have a bad match for the incorrect translational axis and their unanimity is expected to overide the lack of discrimination of weak features and the random quality of the matches of false features.

5.2.2. Utility of the Direction of Translation Sphere

There are significant advantages in defining the error measure with respect to a unit sphere, instead of the potential positions of FOEs and FOCs in the image plane. The sphere is a bounded surface which makes uniform global sampling of the error measure feasible. Additionally, the resolution in the position of the translational axis varies accross the surface of the image plane. For example, the FOEs determined by translational axes seperated by very small angles will be

seperated by larger and larger distances in the plane as intersections of the translational axes and the image plane are placed further from the visible image. The effect of this on the error measure, when it is defined over the image plane, is large flat areas for FOEs further from the visible portions of the image. Finally, special criteria must be used to distinguish between FOEs and FOCs if the error measure is defined relative to the image plane. Roughly parallel image displacements could correspond to an FOE off to one side of the image plane or to an FOC off to the opposite side direction of translation sphere, the corresponding translational axes would be close while on the plane they are completely separated.

5.2.3. Optimization Procedure

The optimization procedure used here is very simple, and, because of the strong unimodality of the error measure and its smoothness, other techniques with more rapid convergence could be used. It is interesting to note, however, that the global component of the optimization performed here is an instance of a generalized Hough Transform [BAL81,0'ROU81] inwhich each feature scales its vote for a particular translational axis by the best match it can find consistent with the translational axis.

5 3 Extensions and Applications

5 3.1. Other Cases of Restricted Motion

The procedure developed in this paper is applicable to other cases of unknown but restricted camera motions for which it is computationally feasible to search directly through a subspace of the camera motion parameters to determine feature matches. Two particular cases are pure sensor rotation and motion constrained to a known plane.

parameters. Two for the axis of rotation and one for the extent of rotation about the axis. In this case, the error measure would be defined with respect to a unit sphere inwhich each point corresponds to an axis of rotation. For each rotational axis, the extent of displacement for image features is determined by different rotations about the axis. There is the additional constraint in the rotational case that the displacements of all features must correspond to the same extent of rotation.

During arbitrary sensor motion relative to a stationary environment, the image motion due to distant environmental points is primarily due to the rotational component of sensor motion. Sensor rotation can be recovered by applying the observer rotation processing procedure to the images of such distant points. The rotation can then be subtracted out to

yield successive images related by sensor translation only.

These resulting images can then be processed by the techniques here.

5.3.2. Multiple Independently Maying Objects

The processing here has been limited to a camera moving relative to a stationary environment, or a stationary camera with a stationary background and a single moving object useful extension would allow for several independently moving objects with different directions of translation technique of summation of errors in feature matching only allows a single axis of translation to be determined and will cause the analysis of the several objects in independent motion to be confounded. Due to the similarity of the global search and a generalized Hough transform noted above, the suggested techniques for decomposing generalized Hough objects transforms into constituient having different parameter values (ADI82, BAL81, O'ROU81] may be applicable

Another approach is to segment an image into regions which potentially correspond to objects, or to arbitrarily divide the image into regular overlapping subimages and perform the translational analysis for each region or subimage independently [WIL80, NAG79]. Experiments have shown it is possible to work with small image areas, at a size comparable to extracted regions or subimage areas, and still determine

the axis of translation with a reasonable level of precision. If objects with similar translations correspond to several different regions or image subareas, then similar translational axes will be determined for these regions or subimages. If objects with different translations correspond to the same regions or subimages, then there will be poor, indistinct error values for the error function. For this second case, it is necessary to resegment, and redetermine a translational axis.

5 3 3. Stabilized Retina

Translational processing is sufficient for vision-based navigation in a stationary environment if the orientation of the optic sensor can be fixed relative to the environment over time. In this case, sensor motion amounts to a sequence of translations in possibly different directions over time.

A difficulty with such a stabilized retina is that much of the environment would not be observable. This can be corrected by using a set of such stabilized retinas arranged to yield a complete view of space. There would then be no need to rotate the sensor to view a particular environmental point. A possible arrangement of retinal surfaces is a cubical one. One of the retinal planes will always contain an FOE and another will always contain an FOE and motion is right on an edge of the cube and the focal length

independent estimates of the director of translation which conbe integrated

5.3.4. The Local Translational Decomposition

This technique can be extended to less restricted forms of sensor motion by applying the procedure for translational motion to small, overlapping areas across an image surface over a sequence of images. This approximates more general motions as consisting locally of environmental translations interpets local image motion as resulting from environmental translations. The feasibility of this is based upon experiments showing that the direction of translation can be extracted with reasonable precision using small image areas a few features. The resulting description containing associates with a set of image points (or small image areas) the approximated direction of motion of the corresponding environmental points (or small environmental surface area) As a low level representation of environmental motion, this can considerably simplify the recovery of the sensor motion parameters [LAW82]. Ιt can also provide qualitative information concerning the rough direction of motion of objects in a scene.

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It requires no restrictions on the direction of motion, nor the location and shape of environmental objects. It has been applied successfully to real-world image sequences from several different task domains.

The processing consists of two basi eps: Feature Extraction and Search. The feature extraction process pass out small image areas which may correspond to distinguishing parts of environmental objects. The direction of translational motion is then found by a search which determines the image displacement paths along which a measure of feature mismatch is minimized for a set of features. The correct direction of translation will minimize this error measure and also determine the corresponding image displacement paths for which the extracted features match well.

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